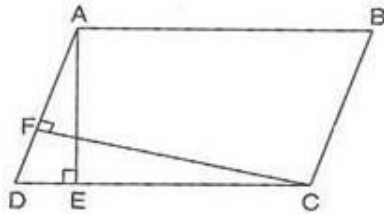
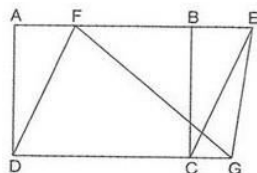


**CBSE Test Paper 03**  
**CH-9 Areas of Parallelograms & Triangles**

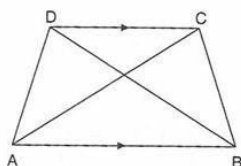
1. ABCD is a parallelogram. If AB = 12 cm, AE = 7.5 cm, CF = 15 cm, then AD is equal to



- a. 3 cm.
  - b. 6 cm.
  - c. 10.5 cm.
  - d. 8 cm.
2. ABCD is a rectangle in which AB = 8 units and AD = 3 units. If DCEF is a parallelogram, then the area of  $\triangle EFG$  is

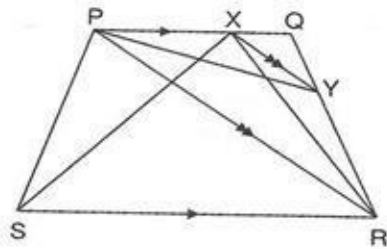


- a. 16 sq units.
  - b. 24 sq units.
  - c. 12 sq units.
  - d. 6 sq units.
3. ABCD is a trapezium in which  $AB \parallel DC$ . If  $ar(\triangle ABD) = 24 \text{ cm}^2$  and AB = 8 cm, then the height of  $\triangle ABC$  is



- a. 4 cm.
- b. 6 cm.
- c. 3 cm.
- d. 8 cm.

4. PQRS is a trapezium with  $PQ \parallel SR$ . A line parallel to PR intersects PQ at X and QR at Y. If  $ar(\triangle PYR) = 5 \text{ cm}^2$ , then  $ar(\triangle PXS)$  is

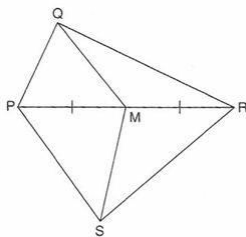


- a.  $5 \text{ cm}^2$ .
- b.  $2.5 \text{ cm}^2$ .
- c.  $10 \text{ cm}^2$ .
- d.  $7.5 \text{ cm}^2$ .

P

E

5. In quadrilateral PQRS, M is the mid-point of PR. If  $ar(\text{SMQR})$  is  $18 \text{ cm}^2$ , then  $ar(\text{PQMS})$  is



- a.  $12 \text{ cm}^2$ .
- b.  $36 \text{ cm}^2$ .
- c.  $18 \text{ cm}^2$ .
- d.  $24 \text{ cm}^2$ .

6. Fill in the blanks:

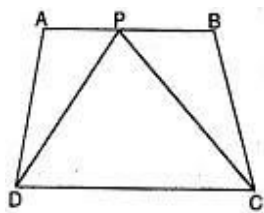
The median of a triangle divides it into two triangles of\_\_\_\_\_.

7. Fill in the blanks:

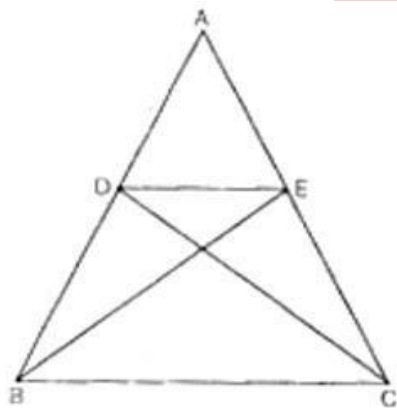
Two triangles having the same base and equal areas lie between the\_\_\_\_\_.

8. The diagonal of a square is 10 cm. Find its area.

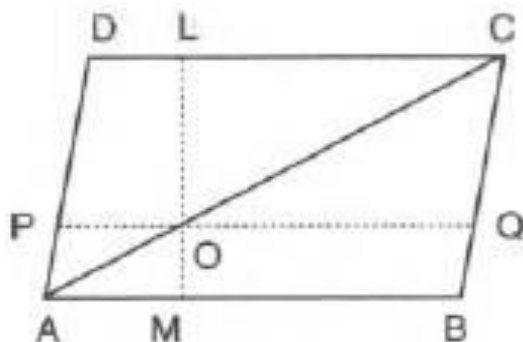
9. Is the given figure lie on the same base and between a same parallels. In such a case, write the common base and the two parallels.



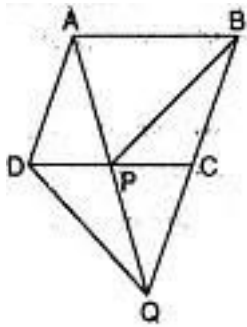
10. D and E are points on sides AB and AC respectively of ABC such that  $ar(DBC) = ar(EBC)$ . Prove that  $DE \parallel BC$ .



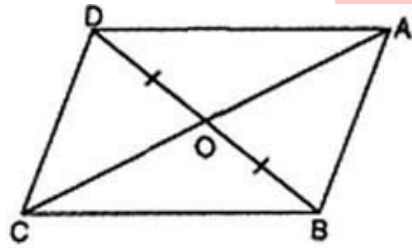
11. In the figure, ABCD is a  $\parallel^{\text{gm}}$ . O is any point on AC.  $PQ \parallel AB$  and  $LM \parallel AD$ . Prove that  $ar(\parallel^{\text{gm}} DLPO) = ar(\parallel^{\text{gm}} BMOQ)$ .



12. Diagonals AC and BD of a trapezium ABCD with  $AB \parallel DC$  intersect each other at O. Prove that  $\text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$ .
13. A point O inside a rectangle PQRS is joined to the angular points. Prove that the sum of the areas of two of the triangles so formed is equal to the sum of the other two triangles.
14. In figure, ABCD is a parallelogram and BC is produced to a point Q such that  $AD = CQ$ . If AQ intersect DC at P, show that  $\text{ar}(BPC) = \text{ar}(DPQ)$ .



15. In figure, diagonals AC and BD of quadrilateral ABCD intersect at O such that  $OB = OD$ .



If  $AB = CD$ , then show that :

- i.  $\text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$
- ii.  $\text{ar}(\triangle DCB) = \text{ar}(\triangle ACB)$
- iii.  $DA \parallel CB$  or ABCD is a parallelogram.

**CBSE Test Paper 03**  
**CH-9 Areas of Parallelograms & Triangles**

**Solution**

1. (b) 6 cm.

**Explanation:**

Here, Area of parallelogram ABCD with base AB =  $AB \times AE = 12 \times 7.5 = 90$  sq. cm

Therefore, Area of parallelogram ABCD with base AD = 90 sq. cm

$$\Rightarrow AD \times CF = 90$$

$$\Rightarrow AD \times 15 = 90$$

$$\Rightarrow AD = 6 \text{ cm}$$

2. (c) 12 sq units.

**Explanation:**

Area of rectangle ABCD =  $8 \times 3 = 24$  sq. cm

Since rectangle ABCD and parallelogram DCEF are on the same base CD and between the same parallels, therefore,

$$\text{area}(\text{ABCD}) = \text{area}(\text{||gmDCEF}) = 24 \text{ sq. cm}$$

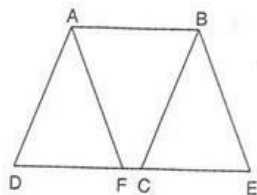
Also, triangle EFG and parallelogram DCEF are on the same base EF and between the same parallels, therefore,

$$\text{area}(\triangle EFG) = \frac{1}{2} \times \text{area}(\text{||gmDCEF}) = \frac{1}{2} \times 24 = 12 \text{ sq. cm}$$

3. (b) 6 cm.

**Explanation:**

In the given figure,



$$\text{area}(\triangle ABD) = \text{area}(\triangle ABC)$$

$$\Rightarrow \text{area}(\triangle ABC) = 24 \text{ Sq. cm}$$

$$\Rightarrow \frac{1}{2} \times AB \times \text{Height of area}(\triangle ABC) = 24$$

$$\Rightarrow \frac{1}{2} \times 8 \times \text{Height of area}(\triangle ABC) = 24$$

$\Rightarrow$  Height of area ( $\triangle ABC$ ) = 6 cm

4. (a)  $5 \text{ cm}^2$ .

**Explanation:**

Since triangle PXS and and PXR are on the same base PX and between the same parallels, the

$\text{area} (\triangle PXS) = \text{area} (\triangle PXR) \dots\dots(i)$

Similarly,  $\text{area} (\triangle PRY) = \text{area} (\triangle PXR) \dots\dots(ii)$

From eq.(i) and (ii), we have

$\text{area} (\triangle PXS) = \text{area} (\triangle PRY)$

$\Rightarrow \text{area} (\triangle PXS) = 5 \text{ cm}^2$

5. (c)  $18 \text{ cm}^2$ .

**Explanation:**

Since M is mid-point of PR, therefore, QM is the median of triangle PQR.

$\Rightarrow \text{area} (\triangle PQM) = \text{area} (\triangle QMR) \dots\dots\dots(i)$

Similarly,  $\text{area} (\triangle PSM) = \text{area} (\triangle SMR) \dots\dots\dots(ii)$

Adding eq.(i) and (ii), we have

$\text{area} (\triangle PQM) + \text{area} (\triangle PSM) = \text{area} (\triangle QMR) + \text{area} (\triangle SMR)$

$\Rightarrow \text{area} (\triangle PQMS) = \text{area} (\triangle PQMS)$

$\Rightarrow \text{area} (\triangle PQMS) = 18 \text{ cm}^2$

6. equal area

7. same parallels

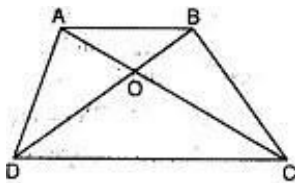
8. Diagonal of a square =  $\sqrt{2}a$

$\Rightarrow 10 = \sqrt{2}a$

$\Rightarrow a = \frac{10}{\sqrt{2}}$

$$\text{Area of the square} = a^2 = \left(\frac{10}{\sqrt{2}}\right)^2 = \frac{100}{2} = 50 \text{ cm}^2.$$

9.  $\triangle PDC$  and quadrilateral  $ABCD$  lie on the same base  $DC$  and between the same parallels  $DC$  and  $AB$ .
10. Given:  $\text{ar}(\triangle DBC) = \text{ar}(\triangle EBC)$   
 To prove:  $DE \parallel BC$   
 Proof: Since two triangles of equal area have common base  $BC$ . Therefore  $DE \parallel BC$   
 [∵ Two triangles having same base (or equal bases) and equal areas lie between the same parallel]
11. Since a diagonal of a parallelogram divides it into two triangles of equal area.  
 $\therefore \text{ar}(\triangle ADC) = \text{ar}(\triangle ABC)$   
 $\Rightarrow \text{ar}(\triangle APO) + \text{ar}(\parallel^{\text{gm}} \text{DLOP}) + \text{ar}(\triangle OLC) = \text{ar}(\triangle AOM) + \text{ar}(\parallel^{\text{gm}} \text{BMOQ}) + \text{ar}(\triangle OQC) \dots \text{(i)}$   
 Since,  $AO$  and  $OC$  are diagonals of parallelograms  $AMOP$  and  $OQCL$  respectively.  
 $\therefore \text{ar}(\triangle APO) = \text{ar}(\triangle AOM) \dots \text{(ii)}$   
 and,  $\text{ar}(\triangle OLC) = \text{ar}(\triangle OQC) \dots \text{(iii)}$   
 Subtracting (ii) and (iii) from (i), we get  
 $\text{ar}(\parallel^{\text{gm}} \text{DLOP}) = \text{ar}(\parallel^{\text{gm}} \text{BMOQ})$
12. Given: Diagonals  $AC$  and  $BD$  of a trapezium  $ABCD$  with  $AB \parallel DC$  intersect each other at  $O$ .



To Prove :  $\text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$

Proof :  $\triangle ABD$  and  $\triangle ABC$  are on the same base  $AB$  and between the same parallels  $AB$  and  $DC$ .

$\therefore \text{ar}(\triangle ABD) = \text{ar}(\triangle ABC) \dots$  [Two triangles on the same base and between the same parallels are equal in area]

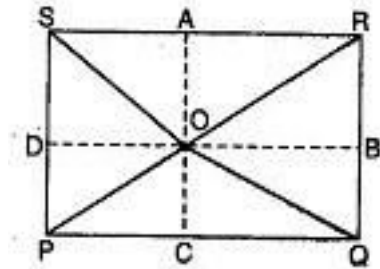
$\Rightarrow \text{ar}(\triangle ABD) - \text{ar}(\triangle AOB) = \text{ar}(\triangle ABC) - \text{ar}(\triangle AOB) \dots$  [Subtracting the same areas from both sides]

$\Rightarrow \text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$

13. Given: A point O inside a rectangle PQRS is joined to the angular points P, Q, R, S.

To Prove :  $\text{ar}(\triangle POQ) + \text{ar}(\triangle ROS) = \text{ar}(\triangle POS) + \text{ar}(\triangle QOR)$

Construction : Draw  $OA \perp RS$ ,  $OB \perp RQ$ ,  $OC \perp PQ$  and  $OD \perp PS$ .



Proof :  $\text{ar}(\triangle POQ) = \frac{(PQ)(OC)}{2}$

$\text{ar}(\triangle ROS) = \frac{(SR)(OA)}{2} = \frac{(PQ)(OA)}{2} \dots$  [As  $SR = PQ$  ... opp. sides of rectangle]

$\therefore \text{ar}(\triangle POQ) + \text{ar}(\triangle ROS) = \frac{(PQ)(OC)}{2} + \frac{(PQ)(OA)}{2}$

$= \frac{(PQ)(OC+OA)}{2} = \frac{(PQ)(AC)}{2} \dots(1)$

Similarly,

$\text{ar}(\triangle QOR) = \frac{(RQ)(OB)}{2}$

$\text{ar}(\triangle POS) = \frac{(PS)(OD)}{2} = \frac{(RQ)(OD)}{2} \dots$  [As  $PS = RQ$  opp. sides of rectangle]

$\therefore \text{ar}(\triangle QOR) + \text{ar}(\triangle POS) = \frac{(RQ)(OB)}{2} + \frac{(RQ)(OD)}{2}$

$= \frac{(RQ)(OB+OD)}{2}$

$= \frac{(RQ)(BD)}{2} = \frac{(AC)(PQ)}{2} \dots(2)$

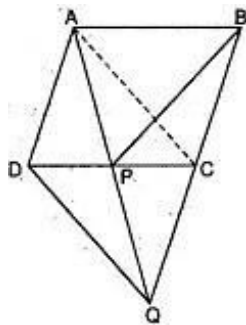
$\text{ar}(\triangle POQ) + \text{ar}(\triangle ROS) = \text{ar}(\triangle QOR) + \text{ar}(\triangle POS) \dots$  [From (1) and (2)]

14. Given: ABCD is a parallelogram and BC is produced to a point Q such that  $AD = CQ$ .

AQ intersects DC at P.

To Prove :  $\text{ar}(\triangle BPC) = \text{ar}(\triangle DPQ)$

Construction : Join AC.



Proof:  $\triangle QAC$  and  $\triangle QDC$  are on the same base QC and between the same parallels AD and QC.

$\therefore \text{ar}(\triangle QAC) = \text{ar}(\triangle QDC) \dots$  [Two triangles on the same base and between the same

parallels are equal] ... (1)

$\Rightarrow \text{ar}(\triangle QAC) - \text{ar}(\triangle QPC) = \text{ar}(\triangle QDC) - \text{ar}(\triangle QPC) \dots$  [Subtracting the same areas from both sides]

$\Rightarrow \text{ar}(\triangle PAC) = \text{ar}(\triangle QDP) \dots (2)$

As  $\triangle PAC$  and  $\triangle PBC$  are on the same base  $PC$  and between the same parallels  $AB$  and  $DC$ .

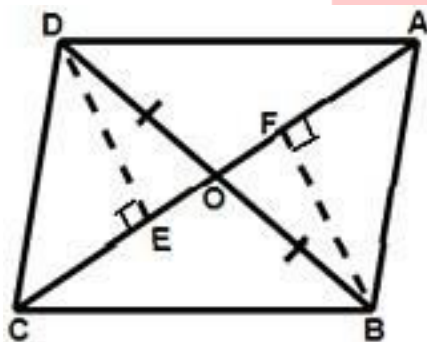
$\therefore \text{ar}(\triangle PAC) = \text{ar}(\triangle PBC) \dots$  [Two triangles on the same base and between the same parallels are equal] ... (3)

$\text{ar}(\triangle PBC) = \text{ar}(\triangle QDP) \dots$  [From (2) and (3)]

$\Rightarrow \text{ar}(\triangle BPC) = \text{ar}(\triangle DPQ)$ .

15. Given: Diagonals  $AC$  and  $BD$  of a quadrilateral  $ABCD$  intersect at  $O$  such that  $OB = OD$ .  
To Prove : IF  $AB = CD$  then,

Construction: Draw  $DE \perp AC$  and  $BF \perp AC$ .



Proof :

$\therefore DA \parallel CB$

$\therefore \text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$

- i.  $\text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$
- ii.  $\text{ar}(\triangle DCB) = \text{ar}(\triangle ACB)$
- iii.  $DA \parallel CB$  or  $ABCD$  is a parallelogram.
- iv. In  $\triangle ADB$ ,

As  $AO$  is a median.

$\therefore \text{ar}(\triangle AOD) = \text{ar}(\triangle AOB) \dots$  [As median of a triangle divides it into two triangles of equal areas] ... (1)

In  $\triangle CBD$ ,

As CO is a median

$\therefore \text{ar}(\triangle COD) = \text{ar}(\triangle COB) \dots$  [As median of a triangle divides it into two triangles of equal areas]  $\dots(2)$

$\text{ar}(\triangle AOD) + \text{ar}(\triangle COD) = \text{ar}(\triangle AOB) + \text{ar}(\triangle COB) \dots$  [Adding (1) and (2)]

$\Rightarrow \text{ar}(\triangle ACD) = \text{ar}(\triangle ACB)$

$\Rightarrow \frac{(AC) \times (DE)}{2} = \frac{(AC) \times (BF)}{2} \dots$  [As area of triangle =  $\frac{\text{Base} \times \text{corresponding altitude}}{2}$ ]

$DE = BF \dots(3)$

In right  $\triangle$ s DEC and BFA,

$DC = BA \dots$  [Given]

$DE = BF \dots$  [From (3)]

$\therefore \triangle DEC \cong \triangle BFA \dots$  [R.H.S. rule]

$\therefore \angle DCE = \angle BAF \dots$  [c.p.c.t.]

But these angles form a pair of equal alternate interior angles.

$\therefore DC \parallel AB$

As  $CD = AB$  and  $DC \parallel AB$

$\therefore$  quadrilateral ABCD is a parallelogram..... [As quadrilateral is a || gm if a pair of opp. sides is parallel and equal]

v. As ABCD is a parallelogram

$OC = OA \dots$  [Diagonals of a parallelogram bisect each other]..... (5)

$\text{ar}(\triangle DOC) = \frac{OC \times DE}{2}$

$\text{ar}(\triangle AOB) = \frac{OA \times BF}{2}$

As  $DE = BF \dots$  [From (3)]

and  $OC = OA \dots$  [From (5)]

vi. From (i)

$\text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$

$\Rightarrow \text{ar}(\triangle DOC) + \text{ar}(\triangle OCB) = \text{ar}(\triangle AOB) + \text{ar}(\triangle OCB) \dots$  [Adding same areas on both sides]

$\Rightarrow \text{ar}(\triangle DCB) = \text{ar}(\triangle ACB)$