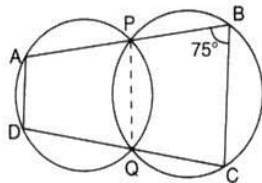


CBSE Test Paper 04

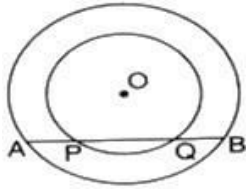
CH-10 Circles

1. The given figure shows two intersecting circles. If $\angle ABC = 75^\circ$, then the measure of $\angle PAD$ is

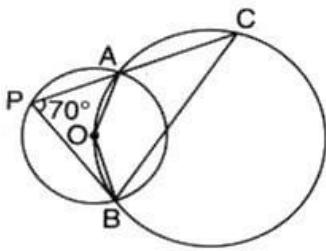


- a. 75°
- b. 105°
- c. 150°
- d. 125°
2. ABCD is a cyclic quadrilateral such that AB is a diameter of the circle circumscribing it and $\angle ADC = 140^\circ$, then $\angle BAC$ is equal to
- a. 40°
- b. 30°
- c. 75°
- d. 50°
3. Two circle are congruent if they have equal.
- a. diameter
- b. chord
- c. radii
- d. secant

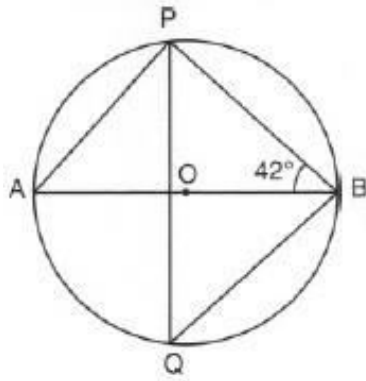
4. If a straight line APQB is drawn to cut two concentric circles, then



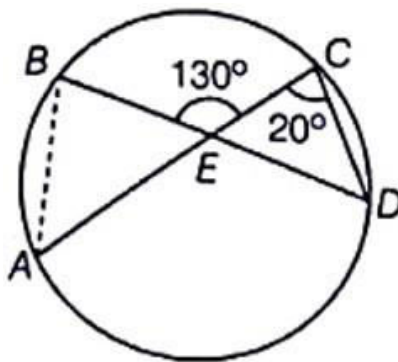
- $AP > BQ$
 - $AP < BQ$
 - $AQ > PB$
 - $AP = BQ$
5. The figure shows two circles which intersect at A and B. The centre of the smaller circle is O and it lies on the circumference of the larger circle. If $\angle APB = 70^\circ$, then the measure of $\angle ACB$ is



- 40°
 - 50°
 - 70°
 - 50°
6. Fill in the blanks:
- The centre of a circle lies in _____ of the circle.
7. In the figure, find $m\angle PQB$ where O is the centre of the circle.



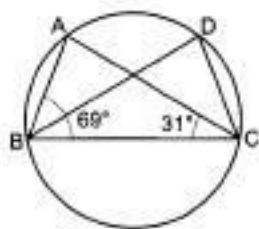
8. Two circles are drawn with sides AB, AC of a triangle ABC as diameters. The circles intersect at a point D. Prove that D lies on BC.
9. In the given figure, A, B, C, and D are four points on a circle. AC and BD intersect at point E such that $\angle BEC = 130^\circ$ and $\angle ECD = 20^\circ$. Find $\angle BAC$.



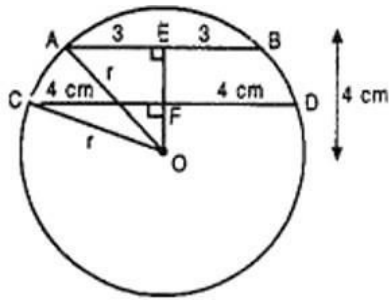
P

E

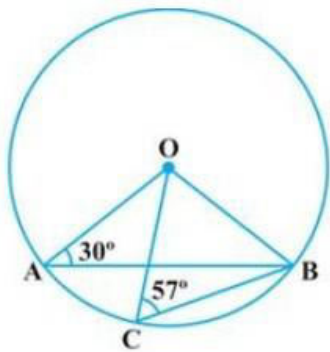
10. In given figure, $\angle ABC = 69^\circ$, $\angle ACB = 31^\circ$, find $\angle BDC$.



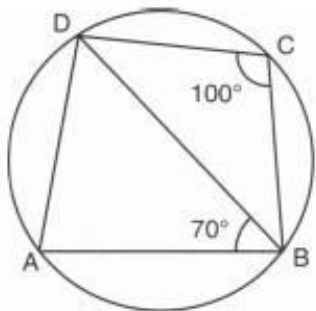
11. The lengths of two parallel chords of a circle are 6 cm and 8 cm. If the smaller chord is at the distance of 4 cm from the centre, what is the distance of the other chord from the centre?



12. $\angle OAB = 30^\circ$ and $\angle OCB = 57^\circ$. Find $\angle BOC$ and $\angle AOC$.



13. In Fig., ABCD is a cyclic quadrilateral. If $\angle BCD = 100^\circ$ and $\angle ABD = 70^\circ$, find $\angle ADB$.



14. If two intersecting chords of a circle make equal angles with the diameter passing through their point of intersection, prove that the chords are equal.

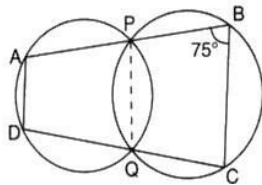
15. PQ and RQ are chords of a circle equidistant from the centre. Prove that the diameter passing through Q bisects $\angle PQR$ and $\angle PSR$.

CBSE Test Paper 04
CH-10 Circles

Solution

1. (b) 105°

Explanation:



Since $\angle PQC + \angle PBC = 180^\circ$ (Opposite angles of a cyclic quadrilateral)

$$\angle PQC = 180^\circ - 75^\circ = 105^\circ$$

Again, $\angle DQP + \angle PQC = 180^\circ$ (Linear Pair)

$$\text{so, } \angle DQP = 75^\circ$$

Also, $\angle PAD + \angle DQP = 180^\circ$ (Opposite angles of a cyclic quadrilateral)

$$\angle PAD = 105^\circ$$

2. (d) 50°

Explanation:

In the given quadrilateral,

$$\angle ABC + \angle ADC = 180^\circ$$

$$140^\circ + \angle ABC = 180^\circ$$

$$\angle ABC = 40^\circ$$

Since, AB is diameter so ABCD lies in semi-circle.

$$\text{thus, } \angle BCA = 90^\circ$$

In triangle, ABC,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle BAC = 180^\circ - 40^\circ - 90^\circ = 180^\circ - 130^\circ = 50^\circ$$

$$\angle BAC = 50^{\circ}$$

3. (c) radii

Explanation:

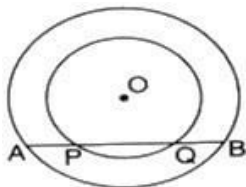


As per theorem,

two circles are congruent only if they have same radii.

4. (d) $AP = BQ$

Explanation:



Let OD is perpendicular to AB. Then $AD = DB$.

Also $DP = DQ$

Therefore, $AP = AD - PD$

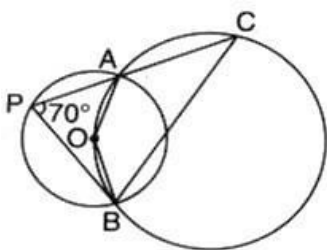
$= BD - DQ$

$= BQ$

Hence, $AP = BQ$

5. (a) 40°

Explanation:



Since, AB is a chord and makes $\angle APB = 70^{\circ}$ at the circumference, so

$$\angle AOB = 140^{\circ}$$

Now, as AOCB is a cyclic quadrilateral then, sum of opposite angles must be 180° .

$$\angle AOB + \angle ACB = 180^{\circ}$$

$$\Rightarrow 140^{\circ} + \angle ACB = 180^{\circ}$$

$$\Rightarrow \angle ACB = 40^\circ$$

6. interior

7. Since angle in a semi-circle is a right angle.

$$\therefore \angle APB = 90^\circ$$

In $\triangle APB$, we have

$$\angle PAB + \angle PBA + \angle APB = 180^\circ$$

$$\Rightarrow \angle PAB + 42^\circ + 90^\circ = 180^\circ$$

$$\Rightarrow \angle PAB = 48^\circ$$

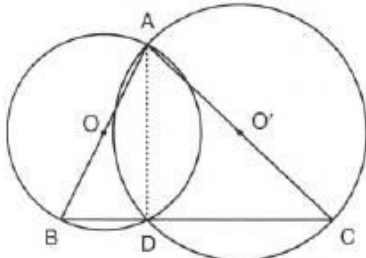
Consider arc BP. We find that $\angle PAB$ and $\angle PQB$ are angles in the same segment of a circle.

$$\therefore \angle PQB = \angle PAB \text{ [}\because \text{Angles in the same segment are equal]}$$

$$\Rightarrow \angle PQB = 48^\circ$$

8. Join AD. Since angle in a semi-circle is a right angle.

$$\therefore \angle ADB = 90^\circ \text{ and } \angle ADC = 90^\circ$$



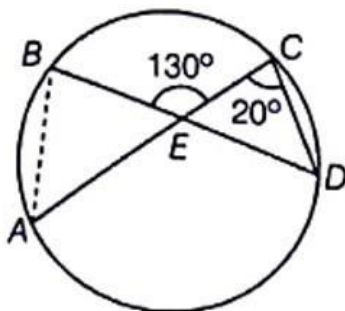
$$\Rightarrow \angle ADB + \angle ADC = 90^\circ + 90^\circ$$

$$\Rightarrow \angle ADB + \angle ADC = 180^\circ$$

$$\Rightarrow \text{BDC is a straight line} \Rightarrow \text{D lies on BC.}$$

9. Given: $\angle BEC = 130^\circ$ and $\angle ECD = 20^\circ$.

To Find : $\angle BAC$



Solution: Since the exterior angle of a triangle is equal to the sum of the interior opposite angles,

$$\therefore \angle BEC = \angle ECD + \angle CDE$$

$$\Rightarrow 130^\circ = 20^\circ + \angle CDE$$

$$\Rightarrow \angle CDE = 130^\circ - 20^\circ = 110^\circ$$

$$\angle BDC = 110^\circ$$

Now, $\angle BAC = \angle BDC$ (Angles in the same segment)

$$\text{Hence } \angle BAC = 110^\circ$$

10. From the given figure, in $\triangle ABC$, we can write

$$\angle ABC + \angle ACB + \angle BAC = 180^\circ \text{ (by angle sum property)}$$

$$69^\circ + 31^\circ + \angle BAC = 180^\circ$$

$$\Rightarrow \angle BAC = 180^\circ - 100^\circ = 80^\circ$$

$$\angle BDC = \angle BAC \text{ (Angles in the same segment)}$$

$$\therefore \angle BDC = 80^\circ$$

11. Let $AB = 6$ cm and $CD = 8$ cm are the chords of circle with centre O .

Join OA and OC .

Since perpendicular from the centre of the circle to the chord bisects the chord.

$$\therefore AE = EB = \frac{1}{2} AB = \frac{1}{2} \times 6 = 3 \text{ cm}$$

$$\text{And } CF = FD = \frac{1}{2} CD = \frac{1}{2} \times 8 = 4 \text{ cm}$$

Perpendicular distance of chord AB from the centre O is OE .

$$\therefore OE = 4 \text{ cm}$$

Now in right angled triangle AOE ,

$$OA^2 = AE^2 + OE^2 \text{ [Using Pythagoras theorem]}$$

$$\Rightarrow r^2 = 3^2 + 4^2$$

$$\Rightarrow r^2 = 9 + 16 = 25$$

$$\Rightarrow r = 5 \text{ cm}$$

Perpendicular distance of chord CD from the center O is OF .

Now in right angled triangle OFC ,

$$OC^2 = CF^2 + OF^2 \text{ [Using Pythagoras theorem]}$$

$$\Rightarrow r^2 = 4^2 + OF^2$$

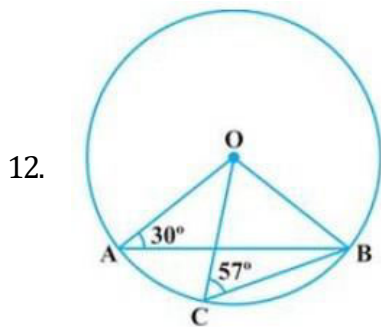
$$\Rightarrow 5^2 = 16 + OF^2$$

$$\Rightarrow OF^2 = 25 - 16$$

$$\Rightarrow OF^2 = 9$$

$$\Rightarrow OF = 3 \text{ cm}$$

Hence distance of other chord from the centre is 3 cm.



In $\triangle OBC$ we have

$$OB = OC \text{ [Radii of the same circle]}$$

$$\therefore \angle OCB = \angle OBC = 57^\circ$$

Now, in $\triangle BOC$, we have

$$\angle OCB + \angle OBC + \angle BOC = 180^\circ$$

$$57^\circ + 57^\circ + \angle BOC = 180^\circ$$

$$\Rightarrow \angle BOC = 180^\circ - 114^\circ = 66^\circ$$

Again, in $\triangle AOB$, we have

$$OB = OA \text{ [Radii of the same circle]}$$

$$\angle OAB = \angle OBA = 30^\circ$$

$$\angle OAB + \angle OBA + \angle AOB = 180^\circ$$

$$\Rightarrow 30^\circ + 30^\circ + (\angle AOC + \angle BOC) = 180^\circ$$

$$\Rightarrow 60^\circ + \angle AOC + 66^\circ = 180^\circ$$

$$\Rightarrow \angle AOC = 180^\circ - 126^\circ = 54^\circ$$

Hence, $\angle BOC = 66^\circ$ and $\angle AOC = 54^\circ$

13. We have, $\angle BCD = 100^\circ$ and $\angle ABD = 70^\circ$

$\therefore \angle DAB + \angle BCD = 180^\circ$ [Opposite angles of cyclic quad.]

$$\Rightarrow \angle DAB + 100^\circ = 180^\circ$$

$$\Rightarrow \angle DAB + 180^\circ - 100^\circ = 80^\circ$$

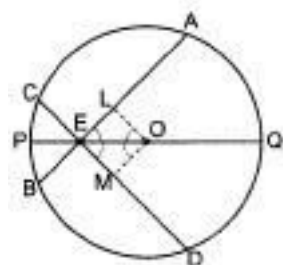
In $\triangle DAB$, by angle sum property,

$$\angle ADB + \angle DAB + \angle ABD = 180^\circ$$

$$\Rightarrow \angle ADB + 80^\circ + 70^\circ = 180^\circ$$

$$\Rightarrow \angle ADB = 180^\circ - 80^\circ - 70^\circ = 30^\circ$$

14.



Given: AB and CD are two chords of a circle with centre O, intersecting at point E. PQ is a diameter through E, such that $\angle AEQ = \angle DEQ$.

To prove: $AB = CD$

Construction: Draw $OL \perp AB$ and $OM \perp CD$

Proof: $\angle LOE + \angle LEO + \angle OLE = 180^\circ$ (Angle sum property of a triangle)

$$\Rightarrow \angle LOE + \angle LEO + 90^\circ = 180^\circ$$

$$\angle LOE + \angle LEO = 90^\circ \dots\dots\dots (i)$$

Similarly, $\angle MOE + \angle MEO + \angle OME = 180^\circ$

$$\Rightarrow \angle MOE + \angle MEO + 90^\circ = 180^\circ$$

$$\angle MOE + \angle MEO = 90^\circ \dots\dots\dots (ii)$$

From (i) and (ii) we get

$$\angle LOE + \angle LEO = \angle MOE + \angle MEO \dots\dots\dots (iii)$$

Also, $\angle LEO = \angle MEO$ (Given) ... (iv)

From (iii) and (iv) we obtain

$$\angle LOE = \angle MOE$$

Now in triangles OLE and OME

$$\angle LEO = \angle MEO \text{ (Given)}$$

$\therefore \angle LOE = \angle MOE$ (Proved above)

$EO = EO$ (Common)

\therefore by ASA congruence criterion we have:

$$\triangle OLE \cong \triangle OME$$

$\therefore OL = OM$ (by CPCT)

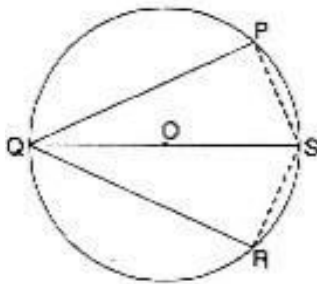
Thus, chords AB and CD are equidistant from the centre O of the circle. Since, chords of a circle which are equidistant from the centre are equal.

$\therefore AB = CD$

15. Given: PQ and RQ are two chords of a circle equidistant from the centre.

To prove: The diameter QS passing through Q bisects $\angle PQR$ and $\angle PSR$.

Construction : Join PS and RS.



Proof : Chords PQ and RQ are equidistant from the centre.

$\therefore PQ = RQ$ | \because chords of a circle equidistant from the centre are equal

Also $\angle QPS = \angle QRS = 90^\circ$ | \because An angle in a semi-circle is a right angle

$\therefore \triangle PQS$ and $\triangle RQS$ are right $\triangle s$

Now in right $\triangle s$ PQS and RQS

$PQ = RQ$ | Proved above

Hyp. $QS = QS$ | Common

$\therefore \triangle PQS \cong \triangle RQS$ | R.H.S. Axiom

$\therefore \angle PQS = \angle RQS$ | c.p.c.t

and $\angle PSQ = \angle RSQ$ | c.p.c.t

i.e. The diameter QS passing through Q bisects $\angle PQR$ and $\angle PSR$ Proved.