

## CBSE Test Paper 04

## CH-2 Polynomials

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1. If  $x + y + z = 9$  and  $xy + yz + zx = 23$ , then the value of  $x^3 + y^3 + z^3 - 3xyz$  is
- 108
  - 209
  - 144
  - 180
2. The coefficient of  $x^3$  in  $2x + x^2 - 5x^3 + x^4$  is
- 1
  - 2
  - 1
  - 5
3. If  $f(x) = x^2 - 5x + 1$ , then the value of  $f(2) + f(-1)$  is
- 2
  - 1
  - 2
  - 1
4. The value of  $(102)^3$  is
- 1820058
  - 1001208
  - 1061280

d. 1061208

5. The possible expressions for the length, breadth and height of the cuboid whose volume is given by  $3x^3 - 12x$  is

a.  $3x$ ,  $(x + 2)$  and  $(x - 2)$

b.  $x$ ,  $(3x + 2)$  and  $(x - 2)$

c.  $x$ ,  $(x + 2)$  and  $(3x - 2)$

d. none of these

6. Fill in the blanks:

If the number of terms of polynomial are 2 and 3, then the corresponding polynomials are called \_\_\_\_\_ and \_\_\_\_\_.

7. Fill in the blanks:

The degree of the zero polynomial is \_\_\_\_\_.

8. Whether the following are zero of the polynomial, indicated against them.  $p(x) = 2x + 1$ ,  $x = \frac{1}{2}$ .

9. Classify as linear, quadratic and cubic polynomials:

$3t$

10. If  $x - \frac{1}{x} = -1$ , find the value of  $x^2 + \frac{1}{x^2}$

11. Write the expanded form of :  $\left(x - \frac{2}{3}y\right)^3$

12. Find the value of  $x^2 + \frac{1}{x^2}$ , if  $x - \frac{1}{x} = \sqrt{3}$ .

13. Find the remainder when  $f(x) = x^3 - 6x^2 + 2x - 4$  is divided by  $g(x) = 3x - 1$ .

14. Without actual division, prove that  $2x^4 + x^3 - 14x^2 - 19x - 6$  is exactly divisible by  $x^2 + 3x + 2$ .

15. Find  $m$  and  $n$ , if  $(x + 2)$  and  $(x + 1)$  are the factors of  $x^3 + 3x^2 - 2mx + n$ .

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**Solution**

1. (a) 108

**Explanation:**

Given:  $x + y + z = 9$  and  $xy + yz + zx = 23$

$$x^3 + y^3 + z^3 - 3xyz = (x + y + z)(x^2 + y^2 + z^2 - xy - yz - zx)$$

$$= (x + y + z) \left[ (x + y + z)^2 - 2xy - 2yz - 2zx - xy - yz - zx \right]$$

$$= (x + y + z) \left[ (x + y + z)^2 - 3xy - 3yz - 3zx \right]$$

$$= (x + y + z) \left[ (x + y + z)^2 - 3(xy + yz + zx) \right]$$

$$= (9) \left[ (9)^2 - 3(23) \right]$$

$$= 9 \times [81 - 69]$$

$$= 9 \times 12$$

$$= 108$$

2. (d) -5

**Explanation:**

The coefficient of  $x^3$  in  $2x + x^2 - 5x^3 + x^4$  is  $-5$ .

3. (a) 2

**Explanation:**

$$f(x) = x^2 - 5x + 1$$

$$f(2) + f(-1)$$

$$= (2)^2 - 5 \times 2 + 1 + (-1)^2 - 5 \times (-1) + 1$$

$$= 4 - 10 + 1 + 1 + 5 + 1$$

$$= 12 - 10$$

$$= 2$$

4. (d) 1061208

**Explanation:**

$$(102)^3 = (100 + 2)^3$$

$$= (100)^3 + (2)^3 + 3 \times 100 \times 2(100 + 2)$$

$$= 1000000 + 8 + 60000 + 1200$$

$$= 1061208$$

5. (a)  $3x$ ,  $(x + 2)$  and  $(x - 2)$

**Explanation:**

To find the length, breadth and height, we will factorize the given polynomial.

$$3x^3 - 12x$$

$$= 3x [x^2 - 4]$$

$$= 3x [x^2 - (2)^2]$$

$$= 3x (x + 2) (x - 2)$$

Therefore, the possible expressions for the length, breadth and height of the cuboid whose volume is given by  $3x^3 - 12x$  are  $3x$ ,  $(x + 2)$  and  $(x - 2)$ .

6. binomial, trinomial

7. not defined

$$8. p\left(\frac{1}{2}\right) = 2\left(\frac{1}{2}\right) + 1 = 1 + 1 = 2 \neq 0$$

$\therefore \frac{1}{2}$  is not a zero of  $p(x)$ .

9.  $3t$

We can observe that the degree of the polynomial ( $3t$ ) is 1. Therefore, we can conclude that the polynomial  $3t$  is a linear polynomial.

10. We have,

$$\begin{aligned} \left(x - \frac{1}{x}\right)^2 &= x^2 + \frac{1}{x^2} - 2 \times x \times \frac{1}{x} \\ \Rightarrow \left(x - \frac{1}{x}\right)^2 &= x^2 + \frac{1}{x^2} - 2 \\ \Rightarrow (-1)^2 &= x^2 + \frac{1}{x^2} - 2 \quad [\because x - \frac{1}{x} = -1] \\ \Rightarrow 1 &= x^2 + \frac{1}{x^2} - 2 \\ \Rightarrow x^2 + \frac{1}{x^2} &= 1 + 2 \\ \Rightarrow x^2 + \frac{1}{x^2} &= 3 \end{aligned}$$

11. 
$$\begin{aligned} \left(x - \frac{2}{3}y\right)^3 &= x^3 - \left(\frac{2}{3}y\right)^3 - 3(x)\left(\frac{2}{3}y\right)\left(x - \frac{2}{3}y\right) \\ &= x^3 - \frac{8}{27}y^3 - 2xy\left(x - \frac{2}{3}y\right) = x^3 - \frac{8}{27}y^3 - 2x^2y + \frac{4}{3}xy^2 \\ &= x^3 - 2x^2y + \frac{4}{3}xy^2 - \frac{8}{27}y^3 \end{aligned}$$

12. According to the question,

$$x - \frac{1}{x} = \sqrt{3}$$

Squaring both the sides,

$$\begin{aligned} \Rightarrow \left(x - \frac{1}{x}\right)^2 &= (\sqrt{3})^2 \\ \Rightarrow x^2 + \frac{1}{x^2} - 2 \times x \times \frac{1}{x} &= 3 \\ \Rightarrow x^2 + \frac{1}{x^2} &= 3 + 2 \\ \Rightarrow x^2 + \frac{1}{x^2} &= 5 \end{aligned}$$

13. We have,  $g(x) = 3x - 1 = 3\left(x - \frac{1}{3}\right)$

Therefore, by remainder theorem when  $f(x)$  is divided by  $g(x) = 3\left(x - \frac{1}{3}\right)$ , the remainder is equal to  $f\left(\frac{1}{3}\right)$ .

Now,  $f(x) = x^3 - 6x^2 + 2x - 4$

$$\Rightarrow f\left(\frac{1}{3}\right) = \left(\frac{1}{3}\right)^3 - 6\left(\frac{1}{3}\right)^2 + 2\left(\frac{1}{3}\right) - 4$$

$$\Rightarrow f\left(\frac{1}{3}\right) = \frac{1}{27} - \frac{6}{9} + \frac{2}{3} - 4 = \frac{1-18+18-108}{27} = -\frac{107}{27}$$

$$\text{Hence, required remainder} = -\frac{107}{27}$$

14. Let  $p(x) = 2x^4 + x^3 - 14x^2 - 19x - 6$  and  $q(x) = x^2 + 3x + 2$

$$\text{Then, } q(x) = x^2 + 3x + 2 = x^2 + 2x + x + 2$$

$$= x(x + 2) + 1(x + 2) = (x + 2)(x + 1)$$

$$\text{Now, } p(-1) = 2(-1)^4 + (-1)^3 - 14(-1)^2 - 19(-1) - 6$$

$$= 2 - 1 - 14 + 19 - 6 = 21 - 21$$

$$p(-1) = 0$$

$$\text{and, } p(-2) = 2(-2)^4 + (-2)^3 - 14(-2)^2 - 19(-2) - 6$$

$$= 32 - 8 - 56 + 38 - 6 = 70 - 70$$

$$p(-2) = 0$$

$\Rightarrow (x + 1)$  and  $(x + 2)$  are the factors of  $p(x)$ , so  $p(x)$  is divisible by  $(x + 1)$  and  $(x + 2)$ .

Hence,  $p(x)$  is divisible by  $(x + 1)(x + 2) = x^2 + 3x + 2$ .

15. Let  $f(x) = x^3 + 3x^2 - 2mx + n$

Since,  $(x + 2)$  and  $(x + 1)$  are the factors of  $f(x)$ .

$$\therefore f(-2) = 0 \text{ and } f(-1) = 0$$

$$\Rightarrow f(-2) = (-2)^3 + 3(-2)^2 - 2m(-2) + n = 0 \text{ and } f(-1) = (-1)^3 + 3(-1)^2 - 2m(-1) + n = 0$$

$$\Rightarrow -8 + 12 + 4m + n = 0 \text{ and } -1 + 3 + 2m + n = 0$$

$$\Rightarrow 4m + n = -4 \dots(i) \text{ and } 2m + n = -2 \dots(ii)$$

On multiplying Eq. (ii) by 2 and then subtracting Eq. (i) from Eq. (ii), we get,

$$4m + 2n - (4m + n) = -4 - (-4) \Rightarrow n = 0$$

On putting  $n = 0$  in Eq. (i), we get  $4m + 0 = -4 \Rightarrow m = -1$

Hence,  $m = -1$  and  $n = 0$ .